

# Leaching of Conductive Species:

## Implications to Measurements of Electrical Resistivity

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### **Abstract**

Electrical tests have been used to characterize the microstructure of porous materials, the measured electrical response being determined by the contribution of the microstructure (porosity and tortuosity) and the electrical properties of the solution (conductivity of the pore solution) inside the pores of the material. This study has shown how differences in concentration between the pore solution (i.e., the solution in the pores) and the storage solution surrounding the test specimen leads to significant transport (leaching) of the conductive ionic species between the pore solution and the storage solution. Leaching influences the resistivity of the pore solution, thereby influencing electrical measurements on the bulk material from either a surface or uniaxial bulk resistance test. This paper has three main conclusions: 1.) Leaching of

conductive species does occur with concentration gradients and that a diffusion based approach can be used to estimate the time scale associated with this change. 2.) Leaching of ions in the pore solution can influence resistivity measurements, and the ratio of surface to uniaxial resistivity can be used as a method to assess the presence of leaching and 3.) An estimation of the magnitude of leaching for standardized tests of cementitious materials.

**Keywords:** electrical properties, resistivity, conductivity, alkali leaching, pore solution, simulation, diffusion; formation factor

## 1 Introduction

Electrical measurements in cementitious systems are gaining increasing use to quantify the transport properties of concrete mixtures[1–9]. Frequently, electrical resistivity is used to determine the ionic transport properties of concrete as it can be related to the chloride ion diffusion coefficient [10,11]. The diffusion coefficient can be used with service-life prediction models to estimate service life of a concrete element [12–14].

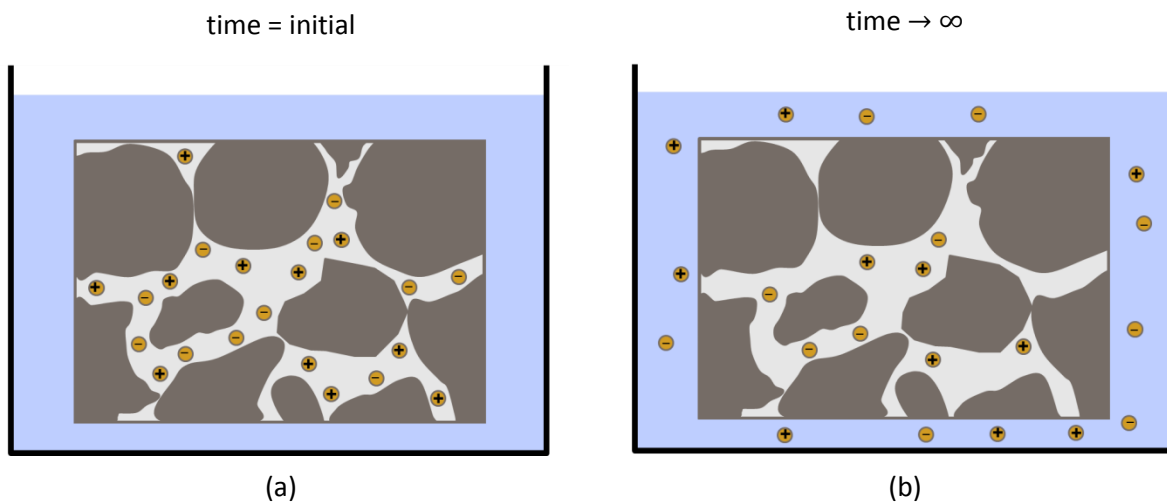
One of the most-often presented equations describing the electrical properties of a fully saturated system is the Nernst-Einstein equation, shown in Equation 1:

$$\frac{\rho_T}{\rho_o} = \frac{D_o}{D} = F = \frac{1}{\phi\beta} \quad [1]$$

where  $\rho_T$  is the bulk concrete resistivity that is a measured parameter,  $\rho_o$  is the pore solution resistivity discussed in detail below,  $D_o$  is the self-diffusion coefficient that describes how a particular ionic species diffuses through a dilute solution and is tabulated for different species for different temperatures [15],  $D$  is the bulk concrete diffusion coefficient that describes the diffusion not considering binding or potential effects,  $F$  is the formation factor,  $\phi$  is the porosity, and  $\beta$  is the inverse of the tortuosity of the porosity (0 to 1) [10,16].

Equation 1 illustrates that the resistivity of the pore solution,  $\rho_o$ , is an important factor when determining the formation factor; it cannot be inferred from bulk resistivity measurements alone. When sealed curing is used in cementitious systems (i.e., when no outside fluid enters or leaves the specimen) the composition of the cementitious materials and the mixture proportions can be used to estimate the pore solution chemistry (species concentrations). This can be used to estimate the pore solution resistivity using a procedure described by Taylor [17] and Snyder et al. [18], and that has also been programmed into a web application by Bentz [19], available at <http://concrete.nist.gov/poresolutioncalc.html>. Numerous research studies have shown a good correlation between this theoretical approach and experimental values, for a sealed sample, for ordinary portland cement (OPC) concretes, e.g. [11,20–24]. The primary concern with sealed specimens is they are not a saturated system, and Equation 1 is generally applied to a saturated system. However, corrections for non-saturated systems (non air-entrained) have been developed [25].

Pore solution measurements on water-cured specimens can exhibit a significant deviation between experimental results and estimates based on the soluble alkalis, e.g. [26]. The web-based model discussed in the preceding paragraph has an option for saturated curing. This option incorporates the effects of saturation by reducing the concentration of the pore solution consistent with additional water being provided to account for the chemical shrinkage, but this approach does not match experimentally obtained results on specimens that are stored under water. This approach does, however, seem to agree with estimates for pore solutions that are expressed from specimens that are sealed cured and then vacuum saturated at time of testing [26]. The authors have hypothesized that this is due to conductive species leaving the pore solution, i.e., leaching, and going into the storage solution. A conceptual illustration of this is shown in Figure 1.



**Figure 1** Conceptual illustration of conductive species in the pore solution of a porous material, a) where no leaching has occurred and b) after leaching has occurred to equalize the concentration differences between the pore and storage solutions.

The likelihood of ionic leaching into the surrounding solution can be evaluated by comparing the concentrations of species within the pore solution and the storage solution. In typical cementitious systems, the pore solution is predominately composed of potassium ( $K^+$ ), sodium ( $Na^+$ ), and hydroxides ( $OH^-$ ) species. An approximate concentration of these ions,  $[K^+]+[Na^+]=[OH^-]$ , can be around 1.2 mol/L, but the exact value depends strongly on the mixture characteristics, the chemistry of the cementitious materials, and the curing age [18]. Conversely, the composition of the storage solution is often much lower in terms of the concentration of these ions. Often, a storage solution of saturated lime-water (calcium hydroxide) is suggested [27], in which case the concentration of  $K^+$  and  $Na^+$  is initially low, and that of  $OH^-$  is not much higher (approximately 0.05 mol/L). If saturated lime-water is not used, calcium hydroxide leaching can take place which can cause an increase in porosity and alter the microstructure. This equates to a large concentration difference between the high concentration pore solution and the low concentration storage solution, which leads to the leaching of ionic species from the pore solution in the sample.

Alkali leaching has been noticed previously in alkali-silica reaction (ASR) studies, as far back as the 1940s [28]. Blanks and Meissner analyzed the water at the bottom of a bucket containing a specimen undergoing ASR expansion, and noticed that the pH of the solution in the bucket varies quite significantly depending on the alkali content of the cementitious materials being tested. A study by Rogers and Hooton [29] used a series of different curing conditions (number of bars and the presence of wicking material) with the same nominal mixture design and evaluated the equivalent alkalis. Their results showed that the alkali concentration of the sample varies widely.

Famy et al. [30] showed that when storing samples in a humidity of 80 % to 100 %, 80 % of the  $K^+$  ions and 60 % of the  $Na^+$  ions can leach within the first ten days. Leaching has also been discussed by Thomas et al. [31] and Rivard et al. [32]. The reduction in alkalis in a test specimen and an increased concentration in a storage container has also been noted by Muberra and Glasser [33], and in a study by Diamond [34] it has been suggested that alkali leaching is the reason that delayed ettringite is seen in laboratory samples but not field structures.

A study by Spragg et al. [24] has highlighted the impact of storage solution volume on electrical measurements, which has been attributed as an artifact of alkali leaching. In a previous study, a simplified linear mass balance approach was used to estimate the change in pore solution resistivity based upon the change in the resistivity of the storage solution [11].

## **2 Research Significance**

The use of electrical measurements as a method for evaluating the transport properties of cementitious materials requires knowledge of both the measured resistivity of the specimen and the resistivity of the pore solution. If leaching occurs, as illustrated in Figure 1, the pore solution concentration (and resistivity) can change by a significant factor as ions migrate from the specimen into the surrounding storage solution. In a study by Spragg [11], this was shown, for the concrete considered, to be a factor of four. In this paper, experiments and modeling are combined to provide insights into the significance and magnitude of the influence of leaching on electrical properties measured in standardized tests.

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### 126   **3           Experimental Details**

127   The experiments employed in this study were conducted in three phases, and are described in  
128   detail below. Phases I and II were used to demonstrate the leaching of the conductive ionic  
129   species and to characterize the leaching process through a diffusion-based analysis. The model  
130   that was developed did not account for binding, dissolution, or secondary reactions. Phase II was  
131   conducted to illustrate the impact of leaching of conductive species from the pore solution on  
132   the relationship between measurements performed on different resistivity test geometries. As  
133   such, materials whose microstructure was relatively homogeneous and well characterized were  
134   used. Furthermore, pore and storage solutions were chosen such that their concentrations could  
135   be measured and monitored during the leaching process. Lastly, Phase III used the diffusion  
136   simulation model developed in the first two phases as a tool to project the extent of alkali  
137   leaching on a standard concrete test cylinder.

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#### 139   **3.1           Phase I: Leaching Demonstration and Characterization**

140   The objective of Phase I of this study was to demonstrate that the leaching of conductive species  
141   does occur, and that a diffusion approach is able to characterize this process. Experiments for  
142   this phase were conducted on thin ceramic disks made from a high-purity aluminum oxide with  
143   an average pore size smaller than 0.5  $\mu\text{m}$  and a total porosity of 38 %, based on mass  
144   measurements of dry and saturated specimens [35]. The specimens had a diameter of 50 mm

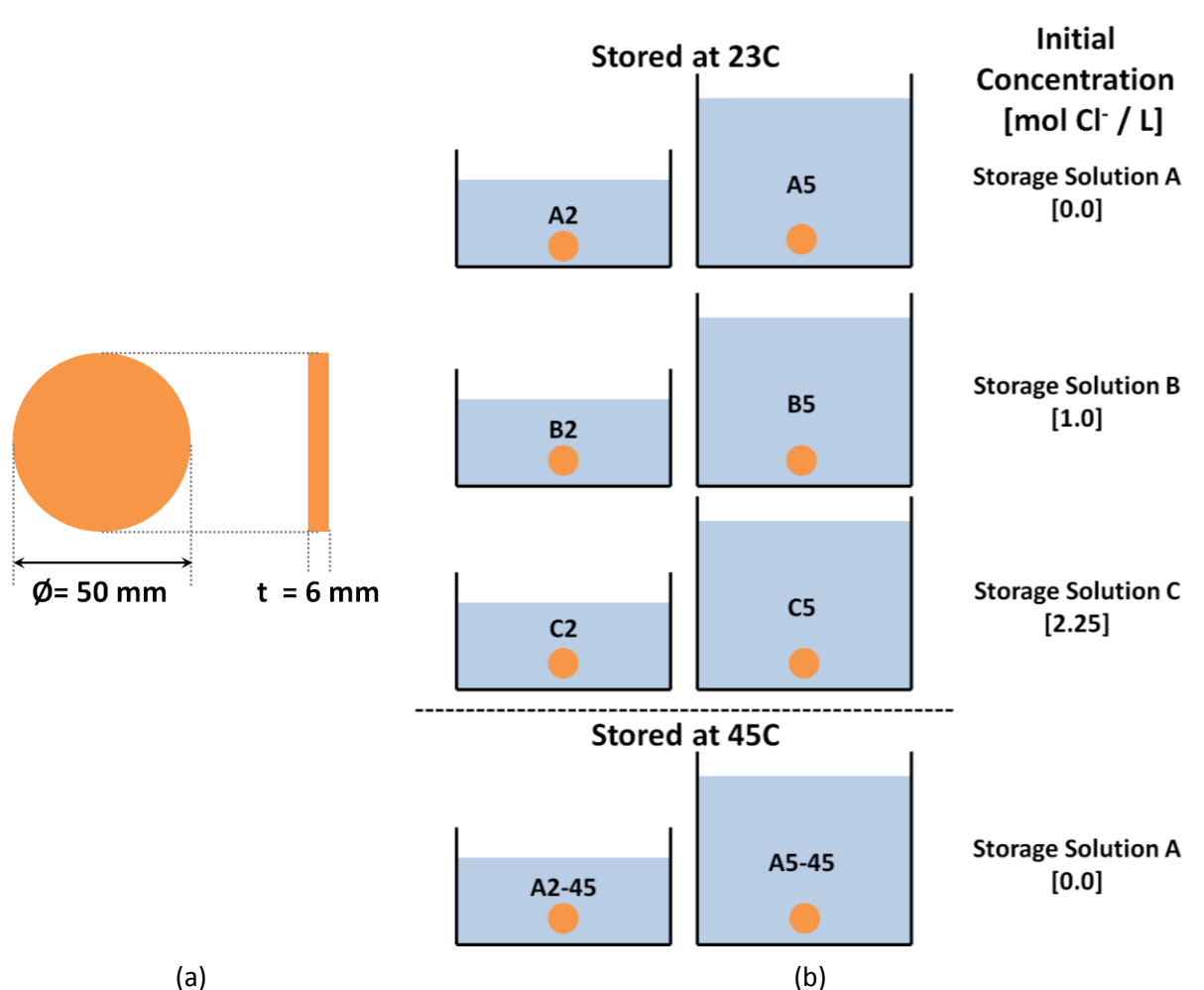
and a thickness of 6 mm. The ceramic was chosen because it had a uniform and non-changing pore structure [35].

The ceramic specimens were vacuum saturated in a solution of potassium chloride (KCl) with a nominal concentration of 7 % KCl by mass. The uniaxial resistivity of the specimens was measured before and after the leaching experiment was conducted.

After vacuum saturation with KCl, the ceramic specimens were measured for electrical resistivity to determine the formation factor, then placed into one of the three following solutions: A) deionized water that is less concentrated than the pore solution; B) 7 % KCl solution by mass, that nominally has the same concentration as the pore solution; or C) 11 % KCl, by mass, which is more concentrated than the pore solution. The storage solution volumes were either twice or five times that of the bulk ceramic disc ( $11.78 \text{ cm}^3$ ) that was placed into the container. It is also worth noting that while the storage solution was twice or five times the bulk volume of the ceramic, the storage volume is 5.3 and 13.2 times larger, respectively, than the volume of pore solution originally contained within the disc, as the pore solution can only occupy the porosity of the disks. Testing was conducted in  $(23 \pm 1)^\circ\text{C}$  or  $(45 \pm 1)^\circ\text{C}$  environments; uncertainties represent one standard deviation. A summary is shown in Figure 2, where the chloride ion ( $\text{Cl}^-$ ) concentrations are given in units of mol/L.



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**Figure 2** Experimental Summary of Phase I using ceramic a.) disc geometry and b.)

concentration and volume of pore solution where A, B, and C describe the concentration of the initial storage solution (smallest to largest), 2 and 5 represent the volume of solution (twice or five times that of the ceramic sample). The pore solution was the same for all conditions at a chloride concentration of 1.0 mol/L.

After the ceramic specimens were placed into their respective storage solutions, the concentration of chloride ions in the storage solution was monitored (as a function of time). In

an effort to be consistent, directly before a measurement was taken, the solution was lightly agitated to help to homogenize the solution. A pipette was used to remove 0.5 mL of solution at the selected time. The 0.5 mL of solution was then titrated using an automatic procedure where small increments of  $\text{AgNO}_3$  solution were added to the solution [36].  $\text{AgNO}_3$  reacts with the  $\text{Cl}^-$  to produce  $\text{AgCl}$  and will subsequently cause a decrease in the conductivity of the solution. When a sufficient amount of  $\text{AgNO}_3$  was added such that the conductivity decreases, stoichiometric calculations can be done based upon the amount of  $\text{AgNO}_3$  added to determine the  $\text{Cl}^-$  concentration in the sample of storage solution [36].

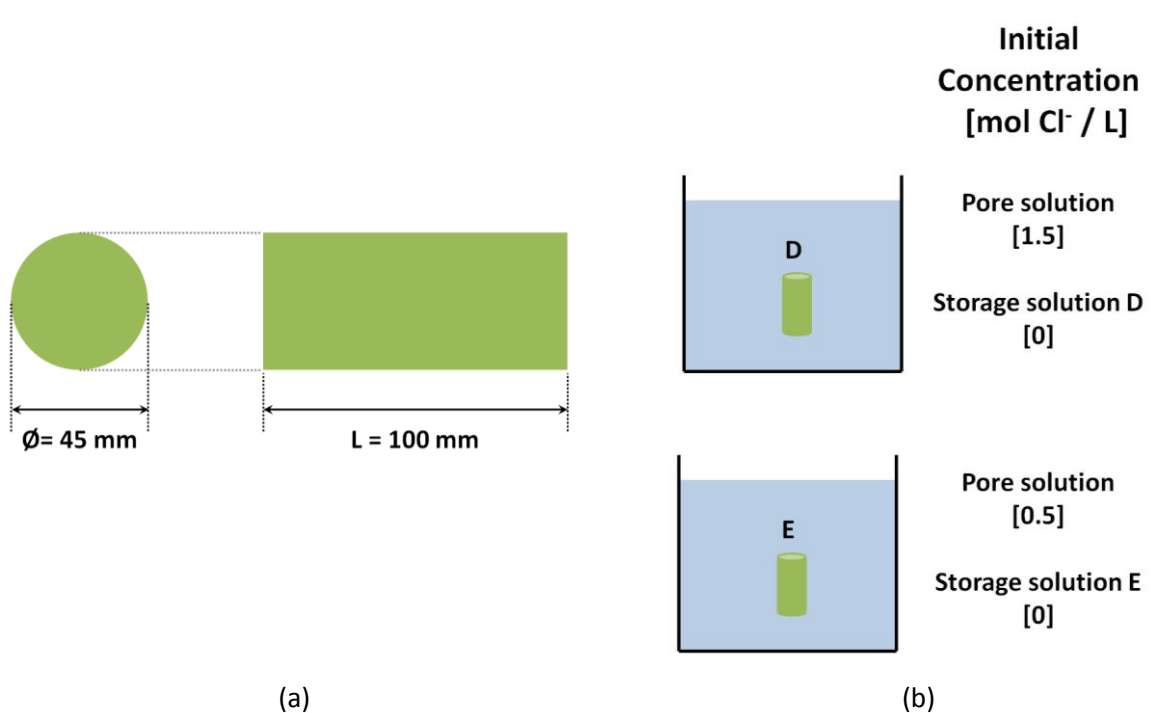
### 3.2 Phase II: Impact on Electrical Measurements

The objective of the Phase II study was to show that leaching of ions in the pore solution can influence resistivity measurements and the relationship between measurements obtained using two different resistivity test geometries. For this phase, testing was conducted on cores taken from an Indiana siltstone. Siltstone was chosen because of its consistent pore structure and its availability [16]. The cores were 45 mm in diameter and were approximately 100 mm in length. Their porosity was measured using vacuum saturation and the difference between dry and saturated masses and was calculated to be  $11.8 \pm 0.2 \%$ , with respect to the dry mass [37].

The siltstone specimens were vacuum saturated with solutions of KCl with nominal concentrations of 5 % and 15 % by mass. The specimens were measured for uniaxial resistivity and surface resistivity, using techniques that have been described previously [22,24]. For surface resistivity, a probe tip spacing of 19 mm was chosen, which is the minimum spacing available for

the equipment used in this study. The resistivity was calculated from the measured resistance and a geometrical correction factor suitable for the tip spacing and the dimensions of the cylinder.

Testing was conducted at  $(23 \pm 1) ^\circ\text{C}$ , and the specimens were stored in deionized water having a volume that was four times the volume of the specimen. As the pore solution leached from the siltstone core, surface and uniaxial resistivity measurements were conducted, as well as measurements taken of the concentration of chloride ions in the storage solution. A summary of the experimental program is shown in Figure 3, where the chloride ion concentrations are given in terms of mol/L.



**Figure 3** Experimental Summary of Phase II Siltstone core a.) dimensions and b.) chloride ion concentration of pore solution and storage solution in mol/L.

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209     3.3           Phase III: Extension to Cementitious Systems

210     Lastly, Phase III of this study provides an estimation of ionic leaching in standard cylindrical  
211     concrete test specimen geometries. This phase of the study investigates how leaching might  
212     influence electrical measurements on a concrete mixtures.

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214     3.4           Testing and Simulation

215     Uniaxial resistivity and the resistivity of solutions were experimentally measured using a Solatron  
216     1260A Impedance Analyzer<sup>1</sup>. Uniaxial measurements of cylinders and discs were accomplished  
217     using plates at the end of the sample and a conductive gel to ensure good electrical contact  
218     between the sample and the electrode. The resistivity of the pore solutions and the storage  
219     solutions was measured using a small solution conductivity cell, whose geometry factor (0.0125  
220     +/- 0.001 m) was determined using a solution of known conductivity. The resistance was tested  
221     using a sinusoidal alternating current in the frequency range of 0.1 Hz to 10 MHz, and the bulk  
222     resistance was determined from the real component of the impedance at the frequency that  
223     minimized the imaginary component of the impedance, as described elsewhere [16,38]. The  
224     geometry factor for both the solutions and the specimens was multiplied by the resistance value  
225     to determine the resistivity. The resistance measurements have a coefficient of variation of 4.36  
226     % [39].

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<sup>1</sup> Certain commercial products are identified in this paper to specify the materials used and procedures employed. In no case does such identification imply endorsement or recommendation by the National Institute of Standards and Technology or Purdue University, nor does it indicate that the products are necessarily the best available for the purpose.

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228 Surface resistivity measurements were performed using an equally-spaced four-probe Wenner  
 229 probe (Proceq Resipod), with an extension kit that allows one to vary the probe spacing. The  
 230 surface resistivity was determined by Equation 2.

231

$$\rho = \frac{V}{I} \cdot \frac{2\pi a}{\hat{k}_2} \quad [2]$$

232

233 where  $I$  is the applied current between the outer probes,  $V$  is the measured voltage difference  
 234 between the inner probes,  $a$  is the probe tip spacing (having units of length), and  $\hat{k}_2$  is a  
 235 dimensionless correction factor to account for specimen size and shape. As discussed in detail by  
 236 Spragg et al. [24], the correction factor  $\hat{k}_2$  was estimated by Morris et al. [40] for cylindrical  
 237 specimens. Values of  $\hat{k}_2$  have been developed for a large range of specimen sizes and probe  
 238 spacings, and are available in the literature [24,40]. It should be noted that, because resistivity is  
 239 an intrinsic material property, it is independent of specimen size or measurement methods.  
 240 Therefore, after applying this correction factor, the ratio of surface to uniaxial resistivities for a  
 241 homogeneous material should be equal to unity [24].

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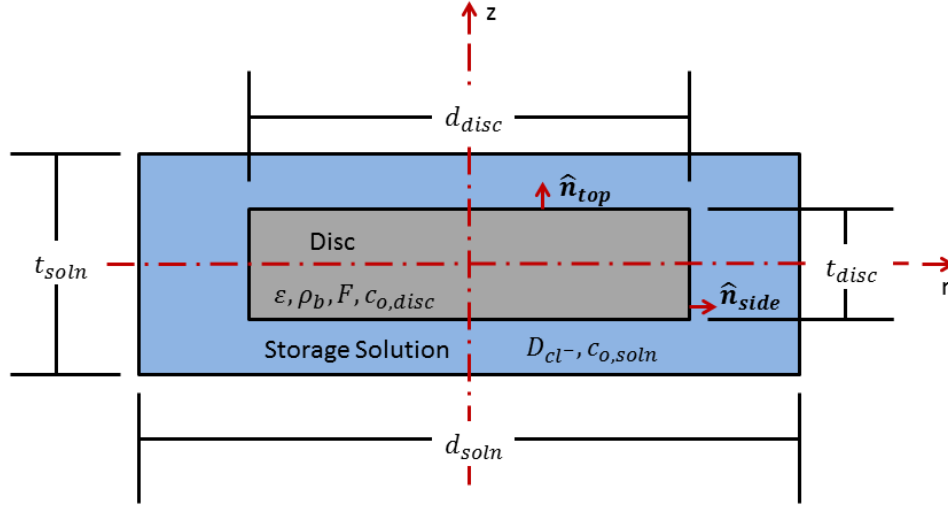
243 The solutions used in Phase I and Phase II were potassium chloride (KCl), which was chosen  
 244 because its concentration, or specifically that of the  $\text{Cl}^-$ , could easily be measured through the  
 245 use of an automated titration machine [36]. Moreover, the electro-chemical mobility of  $\text{K}^+$  and  
 246  $\text{Cl}^-$  are nearly equal, so the diffusion of  $\text{Cl}^-$  in a non-reactive porous material will mimic ideal

Fickian diffusion. A series of concentration measurements conducted to understand the variability of this measurement method indicate a coefficient of variation of 1.5 %.

The leaching of ionic species from the pore solution into the surrounding storage solution can be modeled by a two-dimensional, axis-symmetric geometry (shown in Figure 4 consisting of two regions, the disc and the storage solution. By exploiting the cylindrical symmetry, the calculation domain could be limited to the top right quadrant of the system. This reduces both the complexity of the model and the computation time. The domain was discretized using triangular elements with increased density at the boundary of the disc and storage solution to improve solution convergence and precision. A commercial finite element software package (COMSOL Multi-Physics) was used to solve the transport equations for the disc and storage solution. The software allows the user to specify the triangular mesh density, but automatically determines the appropriate element distribution.

The mathematical model used to describe the transport of chloride ions from the disc to the storage solution can be derived from the continuity equation of a non-deformable, non-reactive porous matrix. A discussion of formulating the continuity equation for diffusion within a porous material can be found elsewhere [41,42] and is reproduced here in Equation 3:

$$\phi \frac{\partial c_i}{\partial t} + (\nabla \cdot \mathbf{J}_i) = 0 \quad [3]$$



**Figure 4** Schematic of two-dimensional, axis-symmetric domain (coordinates  $z$  and  $r$  are shown) used in leaching model; the origin of the coordinate system is located at the center of the sample. Taking advantage of the symmetry of the system, only the top right quadrant was modeled.

In Equation 3,  $c_i$  and  $\mathbf{j}_i$  are the molar concentration and molar flux (moles per unit area of the disk per time) of the  $i^{th}$  species, respectively. The molar flux is given by Fick's first law, Equation 4, which includes the formation factor to account for the porosity and tortuosity of the matrix [41], where  $D_0$  is the self-diffusion coefficient of chloride ions in water [15].

$$\mathbf{j}_i = -\frac{D_0}{F} \nabla c_i \quad [4]$$

The sample is assumed to have constant (in time and space) diffusivity, and has its pore space saturated with a solution containing chloride ions; it is assumed that the degree of saturation did not vary in time. The diffusivity in Equation 4,  $D_0$ , is related to the porosity, connectivity, and

effective diffusivity through Equation 1. Combining Equations 1, 3, and 4 produces Equation 5 that describes the transport of the ionic species through the disc.

$$\phi \frac{\partial c_i}{\partial t} - \nabla \cdot \left( \frac{D_0}{F} \nabla c_i \right) = 0 \quad [5]$$

Equation 5 also describes the transport of chloride ions through the storage solution with the exception that the formation factor and porosity are set to unity. The self-diffusivity of chloride ions in water used in this study, for 25 °C, was  $18.9 \times 10^{-10} \text{ m}^2/\text{s}$  [15,43].

The computational domain is bounded by the two-dimensional plane at  $\theta=0$ , and extends throughout the region  $(0 \leq r \leq R, 0 \leq z \leq Z)$ . The boundary conditions at  $z = 0$  and  $r = 0$  are given in equations 6a and 6b, respectively. The initial chloride concentration is given by the initial condition given in equation 6c.

$$\frac{\partial c_i}{\partial z}(0, r, t) = 0 \quad [6a]$$

$$\frac{\partial c_i}{\partial r}(z, 0, t) = 0 \quad [6b]$$

$$c_i(z, r, 0) = c_{0,disk} \quad [6c]$$

At the interface of the disc and storage solution, continuity between the molar flux leaving the disc and entering the storage solution is assumed. This condition is expressed in Equation 7 where  $\hat{n}_{disc}$  and  $\hat{n}_{solution}$  are the outward pointing normal vectors to the surface of the disk and storage solution, respectively. In Figure 4, when the domain of interest is the ceramic disk and



the flux through the top surface is computed  $\hat{n}_{disk} = \hat{n}_{top}$ . When computing the flux through the side surface of the ceramic disk,  $\hat{n}_{disk} = \hat{n}_{side}$ .

$$\mathbf{j}_{i,disk} \cdot \hat{n}_{disk} = \mathbf{j}_{i,solution} \cdot \hat{n}_{solution} \quad [7]$$

Equation 5 with boundary and initial conditions (Equation 6) and continuity condition (equation 7) were solved over the domain in Figure 4 using the finite element method. An initial time step of 36 s was used and the simulation was run to achieve a total leaching time of  $6.48 \times 10^5$  s (180 h).

The molar flux at the disc-storage solution interface was recorded at each time step. To obtain the number of moles of chloride ions entering the storage solution, the flux was integrated over the top and side surfaces and time as shown in Equation 8. All surface and time integrals were computed in the software package.

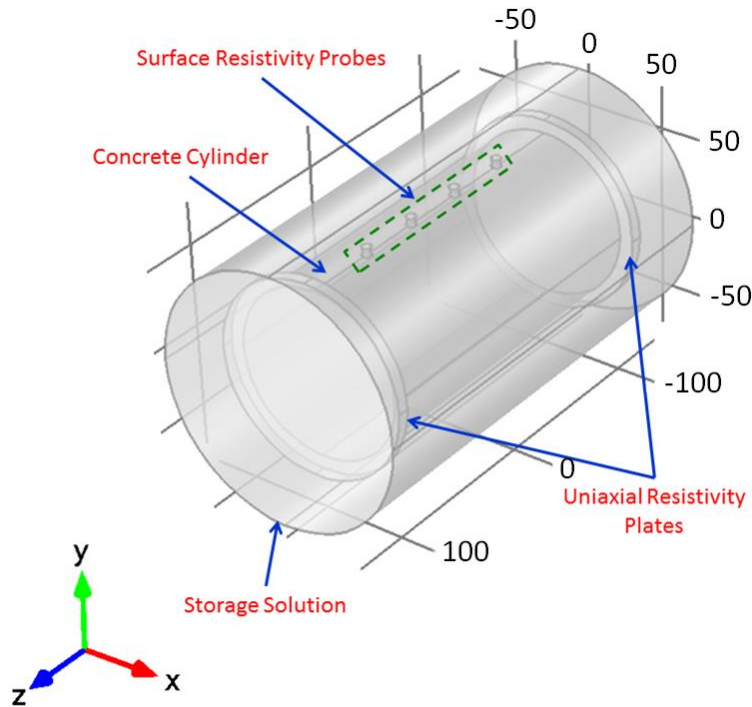
$$q = \int_{t_1}^{t_2} \iint \mathbf{j} \cdot \hat{n} dS dt = \int_{t_1}^{t_2} \iint (\mathbf{j}_{side} \cdot \hat{n}_{side} + \mathbf{j}_{top} \cdot \hat{n}_{top}) dS dt \quad [8]$$

Initial simulations produced long term equilibrium storage solution concentrations that, while consistent with a simple mass balance, were not in agreement with the measured experimental values. Subsequent investigations revealed that this difference was due to sorption (binding) of chloride ions by both the ceramic disc and siltstone substrates. Based on this measured sorption, the initial pore solution concentrations were adjusted appropriately in a second set of simulations, producing the modeling results that are provided in the remainder of this paper.

321

322 The surface and uniaxial resistivity of the siltstone and concrete cylinders is modeled using a  
323 three dimensional (3D) domain. A 2D axi-symmetric model is appropriate to predict the storage  
324 solution concentration as the ion concentration inside the specimen varies along the specimen's  
325 radius and thickness only. This is not the case for the potential field created during a surface  
326 resistivity measurement because there is no axis of symmetry for the surface resistivity test.  
327 Figure 5 shows the geometry used for these calculations. Initially, the sample (without the  
328 surface or end electrodes) is saturated with a concentrated solution. At predetermined time  
329 intervals, the solution concentration in each computation element is used, along with the  
330 formation factor, to calculate the bulk conductivity at each element. Electrodes are added to the  
331 system (with the appropriate boundary conditions for the current flow) and the bulk response is  
332 calculated.

333



**Figure 5** 3D model used to solve for surface and uniaxial resistivity, dimensions given in mm.

When simulating the resistivity measurements, the ion concentration inside the cylinder and the applied voltage potential is important. For the siltstone cylinders, the pore solution is composed of potassium chloride (KCl) dissolved in de-ionized water. The potassium ( $K^+$ ) and chloride ( $Cl^-$ ) species contribute to the resistivity calculations and Equation 5 describes their movement through the cylinder. For concrete, hydroxide ( $OH^-$ ), potassium ( $K^+$ ), and sodium ( $Na^+$ ) are the species that contribute to pore solution conductivity and Equation 5 describes their concentration inside the cylinder over time. The model does not assume electro-diffusion effects of multiple ions in the pore solution. It computes ion concentration of each species independent of other ions.

Calculating the bulk resistivity required solving for the voltage ( $\Phi$ ) everywhere in the system. To do this, one needs to calculate the current flux  $I$  between adjacent computational nodes. The current flux depends upon the electric field ( $E = -\nabla\Phi$ ) and the local conductivity  $\sigma$ :

$$I = \sigma E \quad [9]$$

The local conductivity is a function of local species concentrations in the solution ( $c_i(\mathbf{x})$ ) and the local formation factor:

$$\sigma = \frac{\sigma_{\text{soln}}(c_i(\mathbf{x}))}{F} = \beta \phi \sigma_{\text{soln}}(c_i(\mathbf{x})) \quad [9]$$

In the storage solution,  $\beta = \phi = 1$ .

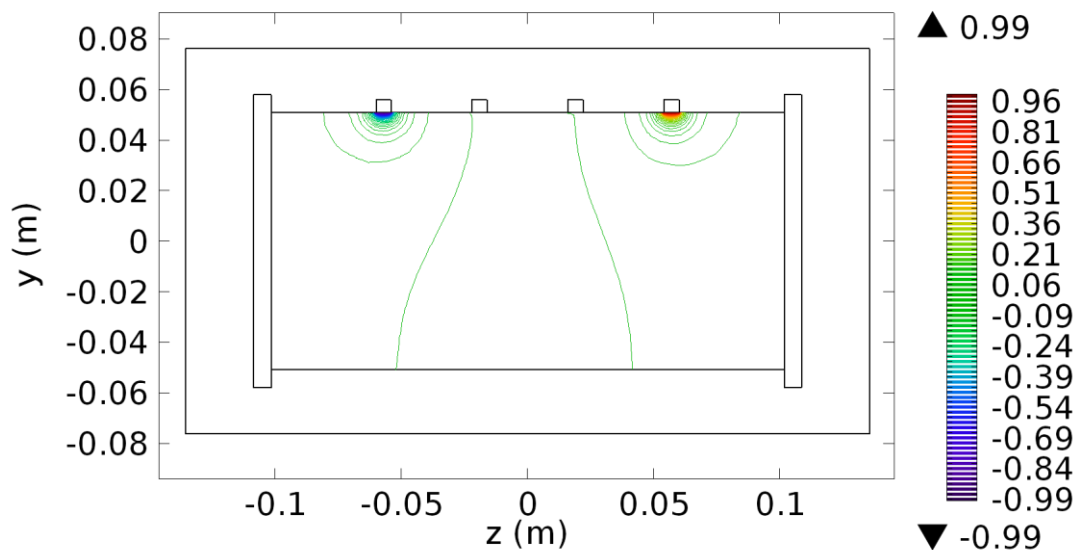
At each point in time during the leaching process, the concentration of the ions in the pore solution is a function of the position inside the cylinder. The ion conductivity is a function of the ion concentration and valence, shown in Equation 12, refer to Snyder et al. [18] for a detailed description of this relationship.

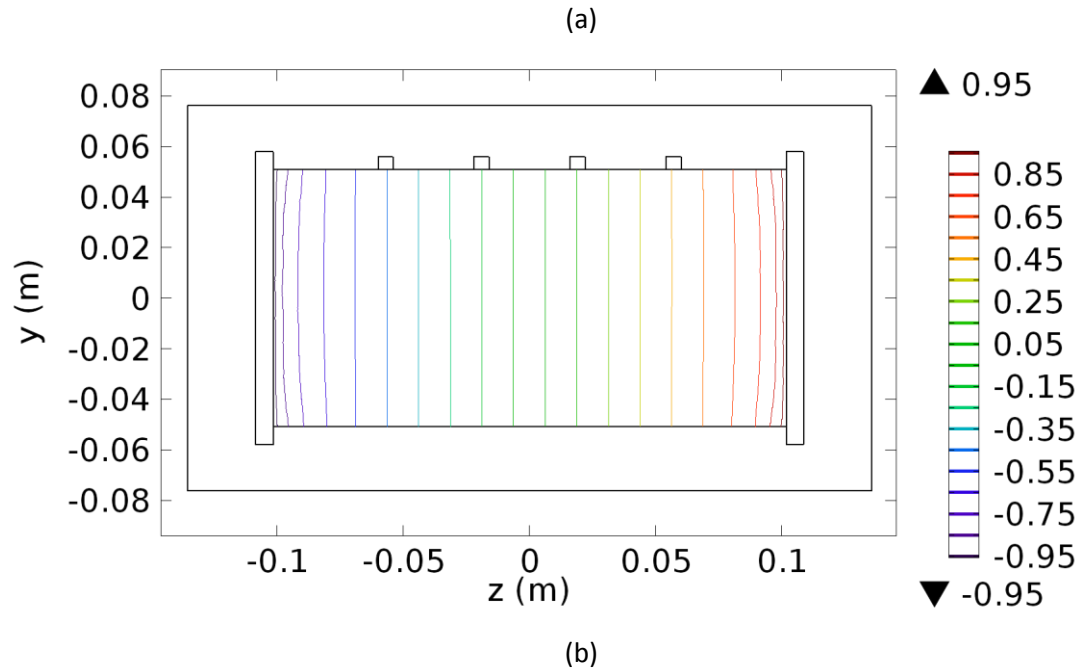
$$\sigma_{\text{soln}} = \sum_i^n z_i c_i \frac{\lambda_i^o}{1 + G_i (1/2 \sum_i^n z_i^2 c_i)^{1/2}} \quad [12]$$

The index  $i$  represents a particular species and goes from 1 to  $n$  species. The quantities  $z_i$  and  $c_i$  are the species valence and molar concentration, respectively. The values  $\lambda_i^o$  and  $G_i$  are the conductivity of the species at infinite dilution and conductivity coefficients (see [18]), respectively.

At each time step in the simulation, Equation 5 determines the ion concentration resulting from the leaching process. The local concentrations are used to solve for the electric potential everywhere. The cylinder resistance is determined in post-processing by computing the current flux through the electrodes (surface probes or end plates). Integrating the current flux over the surface of the electrode is used to calculate the total electrical current. In all simulations a 2 V potential difference is applied (-1 V to 1 V). Applying the appropriate correction factor depending on specimen size and electrode configuration as discussed previously converts the resistance to resistivity.

Figure 6 illustrates the iso-potential surfaces for the surface and uniaxial case of a 100 mm by 200 mm concrete cylinder subjected to leaching for 180 days. At each time-step, the electrode voltages remain the same, but the magnitude of the current flow changes with the changing conductivity.





**Figure 6** Images show lines of constant potential on the y-z plane in side of the concrete cylinder, containing  $\text{OH}^-$ ,  $\text{K}^+$ , and  $\text{Na}^+$  ions, when applying a voltage potential to the a) surface and b) to the ends of the cylinder (uniaxial measurement). The potential lines in (b) are curved near the ends of the cylinder, indicating leaching is occurring from the ends of the cylinder and around its circumference.

#### 4 Results and Discussion

The results from the three phases of this study are described in detail below.

#### 4.1 Phase I: Leaching Demonstration and Characterization

The objective of Phase I was to demonstrate where leaching of conductive species occurs, a diffusion approach could be used to characterize this process. The ceramic discs were saturated with a solution of KCl, which had an experimentally measured resistivity of  $0.135 \Omega \cdot \text{m}$ , while the average uniaxial resistivity of the discs was  $0.552 \Omega \cdot \text{m}$ , which implies a formation factor,  $F_{\text{ceramic}}$ , of  $4.1 \pm 0.5$ .

Once the formation factor of the ceramic was determined, the specimens were placed into different containers containing different storage solutions and storage volumes, as described by Figure 2. The storage solution concentration was monitored during the leaching process, and serves as a measure of how the concentration of the storage solution is changing due to ions leaving the ceramic specimen's pore solution and entering the storage solution.

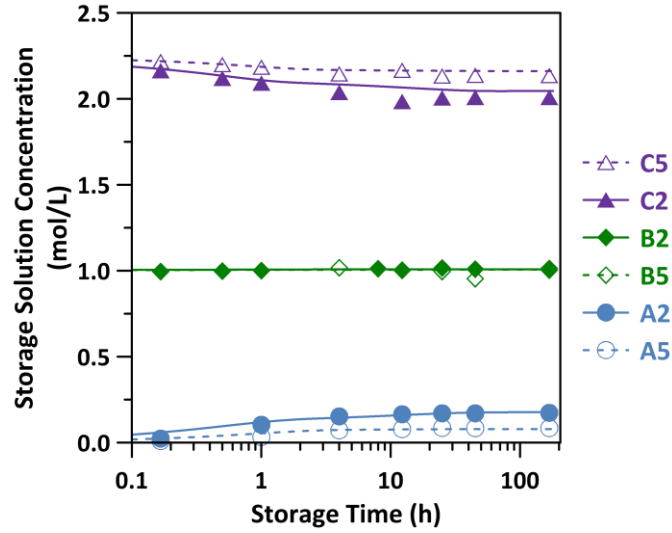
For the specimens placed in the deionized water (Storage Solution A), the initial concentration of the storage solution is zero and increases over time, as shown in Figure 7. As expected, for the larger amount of storage solution surrounding the sample, A5 versus A2, the concentration of the storage solution is lower because the same number of initial ions in the ceramic pore solution must be distributed through a larger total volume of solution (sum of the pores in the ceramic and the volume of storage solution).

For the B series of specimens, the storage solution concentration was chosen to match that of the specimen pore solution, and as expected, the results in Figure 7 indicate that very little

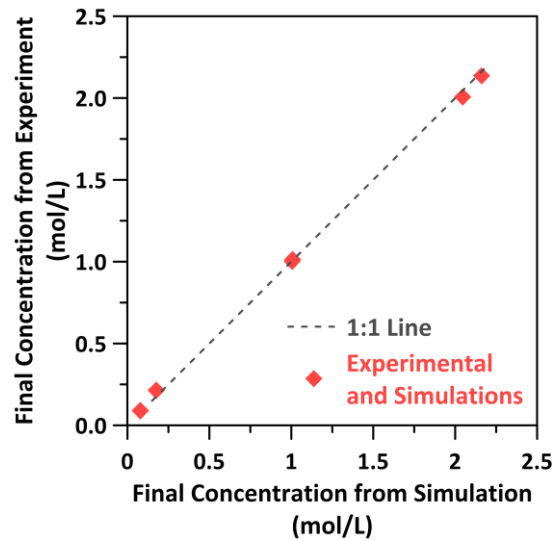
transfer of chloride ions between the two solutions occurred. For the C series, the storage solution chloride ion concentration was higher than that of the specimen pore solution and therefore the concentration of the storage solution decreased over time as in this scenario, chloride ions diffused from the higher concentration storage solution into the lower concentration specimen pore solution.

In general, the agreement between the simulation and the experimental results shown in Figure 7 is reasonable with the average error between the measured and simulated concentration ranging between 16 % to 38 % for the A series specimens, 0.5 % to 1.2 % for the B series specimens, and 0.6 % to 1.7 % for the C series specimens. A mass balance can be employed to calculate the expected final equilibrium concentration of the storage solution and this value would agree with the long-term (> 150 h) simulation results shown in Figure 7 case. The long-term (equilibrium) simulation and experimental results are contrasted in Figure 8, where it can be seen that the ratio between the experimental and simulated equilibrium values is approximately one for all storage solution concentrations measured in this study.



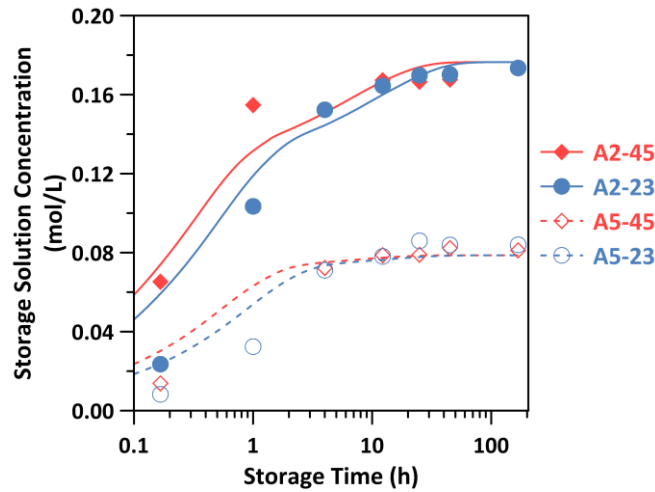


**Figure 7** Concentration of storage solutions as ceramic specimens saturated with a 1 mol  $\text{Cl}^-$  / L solution leached into storage solutions. The initial concentrations of the storage solutions were A) 0.0 mol  $\text{Cl}^-$  / L; B) 1.0 mol  $\text{Cl}^-$  / L; and C) 2.25 mol  $\text{Cl}^-$  / L. Points represent measured concentration, while lines represent data simulations. Concentration measurements have a coefficient of variation of 1.5 %.



**Figure 8** Measured and Final concentration of storage solutions as ceramic specimens saturated with a 1 mol Cl<sup>-</sup> / L solution leached into storage solutions. Points represent measured and simulated results, and the dashed-line represents a perfect one-to-one relationship. Concentration measurements have a coefficient of variation measurement of 1.5 %.

The effect of temperature has also been discussed, as diffusion is a process that is influenced by temperature. As the temperature increases, the diffusion process happens at a faster rate. This is illustrated in Figure 9, by both experimental observations (points) and simulations (lines). The higher temperature (plotted in red and denoted using a suffix of “-45”) show that concentrations reach higher values faster in both storage solution to sample ratio systems. This is illustrated by looking at a storage time along the x-axis, and noticing that the higher temperature data is at a higher value. Furthermore, at a sufficiently long storage time, the concentration of both systems approaches the same concentration. Further research is needed to confirm this effect in cementitious systems, as the solubility of different ionic species can change and reaction rates also need to be considered.



**Figure 9** Concentration of storage solutions for ceramic specimens saturated with a 1 mol Cl<sup>-</sup> / L solution at temperatures of 23 °C (blue) and 45 °C (red), with different volume of storage solutions (denoted with number following letter). Points represent measured concentration, lines represent data simulations. Concentration measurements have a coefficient of variation of 1.5 %.

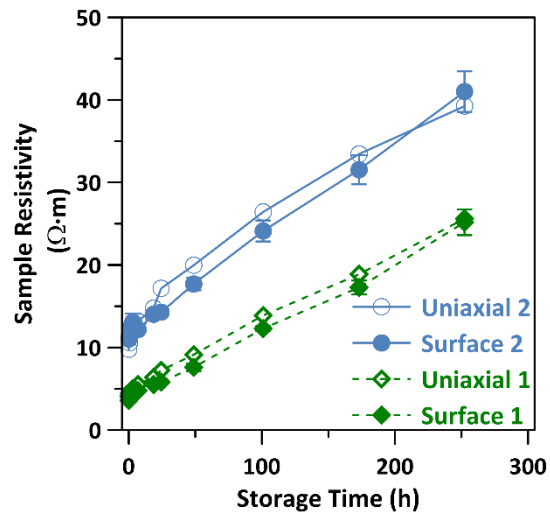
#### 4.2 Phase II: Impact on Electrical Measurements

The objective of Phase II of this study was to illustrate that the leaching of ions in the pore solution can influence the relationship between two different resistivity test geometries, namely uniaxial and surface configurations. Siltstone cores were saturated with KCl solutions, as described in Figure 3. The saturated siltstone cores were placed into solutions of deionized water, and as the leaching process proceeded, the cores were measured for uniaxial and surface resistivity, as shown in Figure 10. The initial resistivity of the cores were divided by the resistivity of the respective pore solutions to determine the average formation factor,  $F_{siltstone}$ , of 55.2 with a standard deviation of 1.6.

468

469 Initially, siltstone specimen 2 had a higher resistivity than specimen 1 because it is saturated with  
 470 a solution that has a higher resistivity. As the time of leaching increases, both surface and uniaxial  
 471 resistivity increase, as the ions in the pore solution leach into the surrounding storage solution.  
 472 The increase in resistivity by a factor of four is only due to increases in the pore solution resistivity  
 473 as the leaching process happens, while the microstructure remains unchanged. This is one reason  
 474 that electrical measurements should be interpreted with consideration of the pore solution.

475



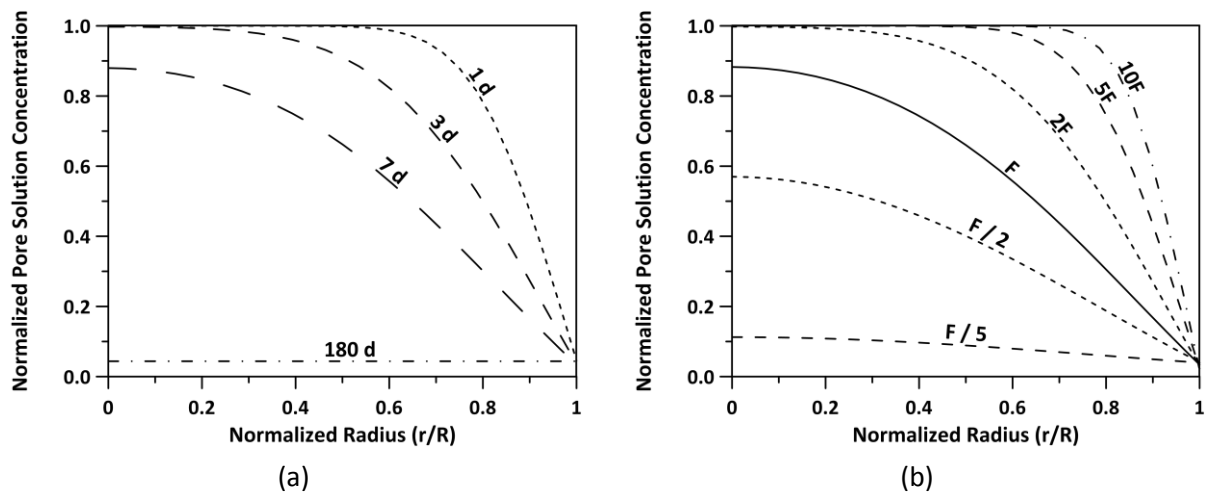
476

477 **Figure 10** Measured resistivity for surface or uniaxial geometry for samples saturated in 1) 1.5  
 478 mol Cl<sup>-</sup> / L and 2) 0.5 mol Cl<sup>-</sup> / L solution and then placed into deionized water for various  
 479 storage times. Error bars represent one standard deviation from the mean.

480

481 The leaching of the conductive species from the siltstone's pore solution into the surrounding  
 482 storage solution can create a layered effect in a cylindrical geometry, with the outer "cylindrical  
 483 shell" in the cylinder consisting of a pore solution of lower ionic concentration than that of the

inner core. Using the diffusion approach from Phase I of this study, this layered effect can be quantified in terms of the ionic concentration profile along the radius of cylinder (near the center of the cylinder), shown in Figure 11. As the concentration is normalized, both the higher concentration and lower concentration pore solutions show a similar trend over time.



**Figure 11** Simulations of pore solution concentration normalized by the concentration before leaching for siltstone specimens as function of the normalized radius (where 0 represents the core and 1 represents the outside surface) for a) the specimens used in this study at increasing leaching times of 1, 3, 7 and 180 d and b) for multiples of the siltstone's formation factor,  $F = 55.2$ , at a leaching time of 7 d.

It can be noticed, even at leaching times up to 3 d, the ionic concentration of the pore solution near the center of the cylinder is similar to the initial concentration. However, the concentration near the surface of the specimen drops quite rapidly. At a leaching time of 7 d, the concentration throughout the entire section of the specimen has decreased measurably. At a leaching time of

180 d, the concentration has nearly become uniform at a very low value corresponding to equilibrium with the leaching (storage) solution.

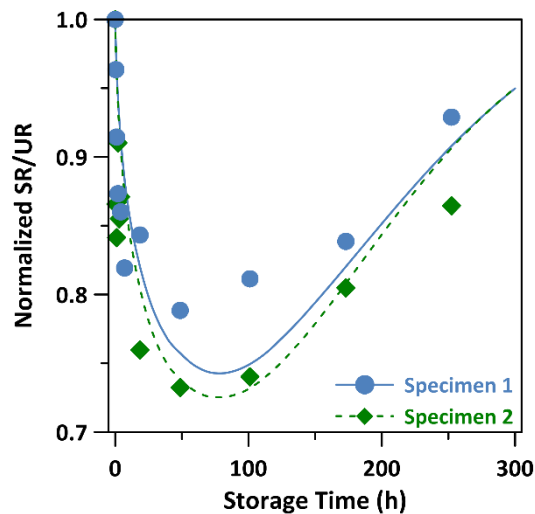
This concentration profile in the radial direction is also influenced by the formation factor of the material, demonstrated in Figure 11b, at an age of 7d. Recall that a higher formation factor represents a less porous material and lower connectivity. The solid curve marked F is using the same formation factor as the siltstone used in this study, 55.2. If the formation factor is decreased, the leaching process happens faster, and the concentration along the radial direction reaches uniformity sooner. Conversely, if the formation factor is increased, the diffusion happens at a slower rate. This creates a higher gradient and also requires a longer time to reach a uniform concentration. It is worth noting, that typical formation factors of regular OPC bridge-deck concretes can be around 500 (or about the 10F line in Figure 11); however, this leaching behavior is still observed, as ion transport is governed by Fick's law with the formation factor only dictating the rate of transport [24].

Previous work has demonstrated how finite layered effects can influence surface and bulk electrical measurements in different ways: half-space [44], or finite slab geometries [11,45–47]. One approach to investigate the effects of layered materials is to study the ratio of surface resistivity to uniaxial resistivity, as originally described by Morris et al. [40]. Recent research has shown that this factor can change as these layered systems evolve [11,48].

Figure 12 presents the ratio of surface resistivity (corrected for geometry according to equation 2) and uniaxial resistivity. The initial experimental and simulation values of the ratio differed slightly (1.12 vs. 0.93), so subsequent measured and simulation values were normalized by the corresponding initial value. The solid points represent experimentally measured values, while the lines represent results from the multiphysics simulation that coupled the diffusion model to obtain the pore solution resistivity gradient and a surface or uniaxial resistivity test. During the initial phase of the leaching process, the ratio decreases. However, after a sufficient amount of time, the ratio begins to increase and again approaches the initial value. This is to be expected because only the initial state and the final steady state are composed of homogeneous (but different) specimens. The specimen during the intermediate phase is relatively heterogeneous, as the leaching of the pore solution leads to an outer core of lower concentration that affects bulk and surface measurements differently. In this experiment, the effect of leaching changed the resistivity ratio by more than 20 %.

While leaching will influence both the uniaxial and surface resistivity, the use of the ratio of surface to uniaxial resistivity appears to be a good method of assessing sample heterogeneity, and the degree to which leaching has happened. It is also important to note that leaching will increase the resistivity of the pore solution in the outer core and will increase both the surface and uniaxial resistivity measurements (shown in Figure 10). For shallow depths of leaching, the ratio of surface to uniaxial resistivity has been shown to be less than unity, mostly due to the large probe spacing that samples the underlying material while the uniaxial resistivity changes more with a more resistive outer layer [45,48–50]. For larger depths of leaching this ratio has

been seen to be higher than unity [48]. When the ratio is close to unity, it can either be assumed that there is no leaching or that sufficient leaching has happened that the material is homogeneous once again. If the ratio differs from 1 by more than 5 %, it can be assumed that leaching is occurring and there is a gradient in the pore solution concentration within the test specimen.



**Figure 12** Ratio of measured surface resistivity to uniaxial resistivity for siltstone specimens saturated with 1) 1.5 mol Cl<sup>-</sup> / L and 2) 0.5 mol Cl<sup>-</sup> / L solution and then placed into deionized water for various storage times. Resistivity measurements have a coefficient of variation of  $\pm 4$  %.

#### 4.3 Phase III: Extension to Cementitious Systems

Phase III of this study will provide an estimation of the effects and magnitude of leaching of pore solution on electrical resistivity measurements on cementitious materials. The concrete material that was modeled was a mixture that had a w/c of 0.4, made with Type I OPC, with a 91 d formation factor of  $420 \pm 95$  and a porosity of  $14.6 \% \pm 0.5 \%$ , which has been characterized by

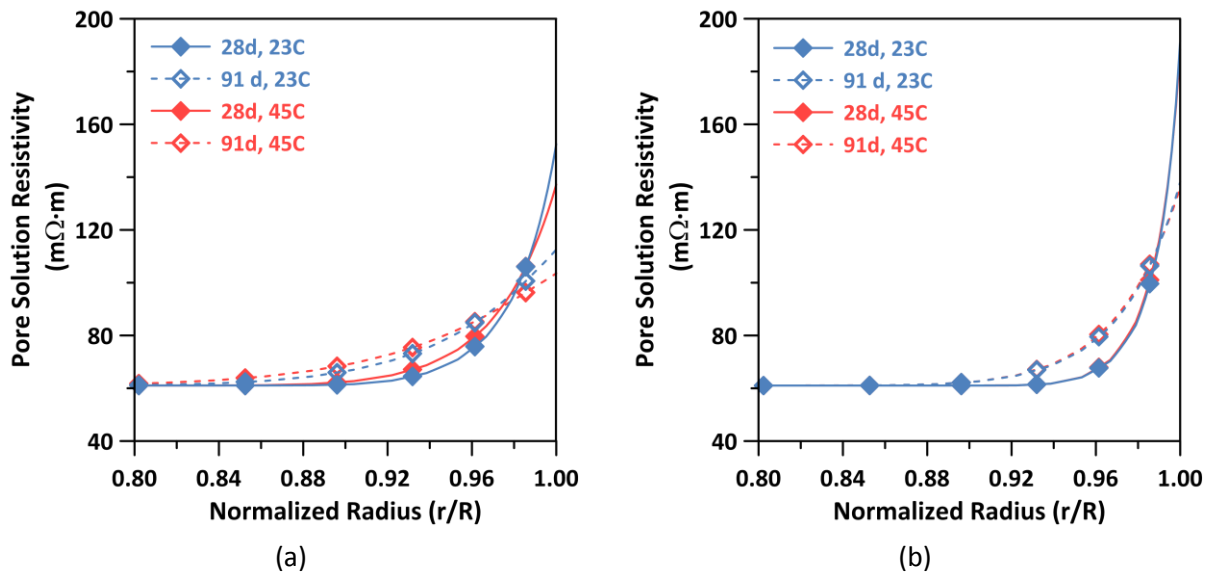


Spragg et al. [51]. The initial concentration of the pore solution was calculated based upon the mixture designs, cement chemistry, and degree of hydration using the online calculator discussed previously [19]. The initial concentration of the storage solution was assumed to be zero.

The multiphysics model that was developed in the first section of the paper is able to describe the diffusion of ionic species based upon the formation factor of the material, and the concentrations of the pore and storage solutions. Of particular importance is the concentration along the radius of the concrete cylinder. The concentration of  $\text{Na}^+$ ,  $\text{K}^+$ , and  $\text{OH}^-$  can be converted to pore solution resistivity, as described by [18]. These results are shown in Figure 13a for a standard 100 mm x 200 mm cylindrical test specimen and Figure 13b for a standard 150 mm x 300 mm cylindrical test specimen. Figure 13 shows calculated pore solution resistivity as a function of the normalized radius ( $r/R$ ), where zero represents the center of the specimen and unity represents the cylinder surface; the symbols represent calculated quantities and the lines guide the eye.

Figure 13 shows that for this hypothetical case, specimens that begin saturated with a known pore solution and are then placed in a solution of low concentration, can develop a measurable pore solution resistivity gradient within 28 d. Note that only the normalized radius from 0.8 to 1.0 is shown, because the resistivity remains relatively constant closer to the center of the cylinder. The resistivity of the pore solution at the surface of test specimen can range from two to three times higher than that inside of the test cylinder. Furthermore, these results suggest that for both 100 mm and 150 mm diameter test cylinders, the leached depth is about 8 mm. This

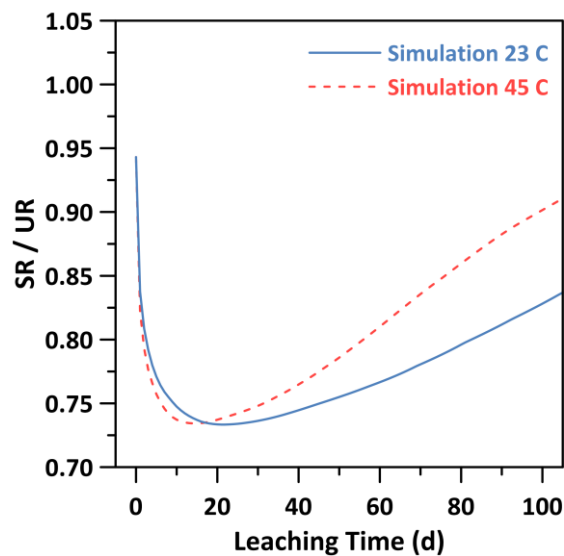
suggests that if specimens must be water-cured, a 150 mm diameter specimen could be cored to a diameter of 130 mm or less before testing with little worry about leaching within the cut volume, even at a curing period of up to 91 d.



**Figure 13** Calculated pore solution resistivity profile at leaching times of 28 and 91 d, at conditioning temperatures of 23 °C and 45 °C, for a) standard 100 mm x 200 mm cylindrical test specimen and b) standard 150 mm x 300 mm cylindrical test specimen. Resistivity measurements have a coefficient of variation of  $\pm 4\%$ .

The gradient shown in Figure 13 will influence resistivity measurements, especially surface resistivity measurements that are sensitive to surface conditions [45,48]. This effect was investigated for each time step using the corresponding gradient, similar to that shown in Figure 13 for 28 d and 91 d, with the second part of the multiphysics model that is able to compare uniaxial and surface resistivity measurements.

The results, shown in Figure 14, illustrate that at a zero leaching time, the ratio of surface to uniaxial resistivity is 0.95, and as the specimen leaches the ratio will decrease. This ratio will reach a minimum (at a point when the specimen has become the most heterogeneous). The value will increase, eventually reaching a value of 1 as the system becomes homogeneous (albeit with a lower pore solution concentration). The specimen at the higher temperature reaches its maximum leached point, the minimum of the dashed line in Figure 14, at an earlier leaching time. The leaching specimen at the higher temperature also has a SR /UR that approaches its initial value at faster rate, which is expected as the higher temperature causes diffusion to occur at a faster rate within the multiphysics model.



**Figure 14** Ratio of surface to uniaxial resistivity for 100 mm x 200 mm cylindrical specimens submerged in tap water at an age of 91 d as the leaching time increases for two different temperatures.

It should be highlighted that both Figure 13 and Figure 14 represent a purely hypothetical case. Specifically, the concrete specimen starts out completely saturated with a known solution, the formation factor remains constant over the leaching period, and there are no binding effects.

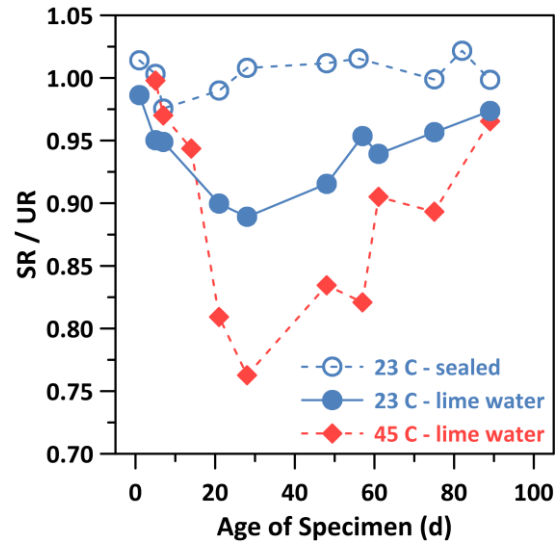
This can be contrasted with typical concrete curing practice, which is to place the specimen in a storage solution consisting of lime saturated water from an early age. For this real life scenario, the previous assumptions do not hold. Specifically, with specimen age: the pore solution is changing concentration due to both leaching and hydration, the formation factor is changing (often several orders of magnitude) due to pore refinement that accompanies hydration of the cementitious materials, and there are changes in the alkali binding behavior of these materials with changes in temperature and degree of hydration. The point being, experimental data that matches the model data is difficult to obtain.

Experimental data presented here is designed to match typical concrete industry curing practices, consequently, the experimental and model data are not directly comparable. However, the conclusions from the experimental data are drawn based on similarities from the model results. Experimental results from concrete specimens, shown in Figure 15, show the ratio of surface to uniaxial resistivity for cylindrical 100 mm x 200 mm concrete specimens that were placed into sealed conditions or lime saturated water at an age of 1 d, at  $(23 \pm 1)^\circ\text{C}$ . After 7 d of curing at  $(23 \pm 1)^\circ\text{C}$  to allow for microstructure development, half of the specimens cured in lime saturated water were placed at  $(45 \pm 1)^\circ\text{C}$ . The specimens were monitored as they aged in their respective curing conditions.

The concrete specimens that are cured under sealed conditions maintain a ratio very close to 1.0, which suggests that no significant leaching takes place in specimens that are sealed cured. Similar results have been observed by Bentz et al. [52] for specimens cured in a 98 % RH environment,

i.e. a moist room. Their data show good agreement between surface and uniaxial resistivity measurements, at ages of 1 d, 7 d, 28 d, and 90 d for a variety of OPC and high-volume fly ash concretes. This is logical, as in both of these cases there is no surrounding storage solution with a significantly lower alkali concentration that drives the leaching of alkalis.

However, moist cured specimens exhibit a decrease in the SR / UR. Specimens that are lime water cured at 23 °C for their entire life, exhibit an initial value close to 1.0 which decreases over time, but eventually will increase again as the specimen experiences sufficient leaching. The SR / UR does not reach as low a value as in the simulations, as the leaching process is occurring concurrently with the decrease in pore solution resistivity due to hydration, and results in a smaller gradient compared to that predicted in the model. The specimens cured at 45 °C exhibit this decrease in SR / UR which is indicative of leaching, but will reach a lower ratio than the specimens cured at 23 °C. This can be due to the elevated temperature increasing the hydration rate, which decreases the resistivity of the pore solution in the inner core, while the increased leaching rate results in a higher resistivity of the pore solution on the outer edge of the specimen. Again, the SR / UR approaches 1.0 for long leaching times.



**Figure 15** Ratio of experimental surface to uniaxial resistivity for 100 mm x 200 mm cylindrical specimens lime-water cured and sealed cured described by Spragg [11] on concrete specimens as they age. Resistivity measurements have a coefficient of variation of  $\pm 4\%$ .

## 5 Summary and Conclusions

Electrical measurements are gaining interest in the concrete industry as a rapid method of characterizing the microstructure. These measurement methods, when combined with information about the pore solution resistivity, can yield information about the specimen diffusivity. This is largely attributed to the use of the Nernst-Einstein relationship, which relates the measured resistivity to ion diffusion coefficients. However, proper information is needed regarding the pore solution resistivity. Previous research has demonstrated that there are dependencies on the volume of storage solution surrounding the specimens [24] and the type of storage solution [11]. These dependencies have been attributed to the leaching of the conductive ionic species from the pore solution.

This study has investigated the leaching of conductive species from a pore solution into the surrounding storage solution. The study began by demonstrating that ionic leaching occurs, with the use of ceramic disks. The specimens were saturated with solutions of potassium chloride, and were placed into storage solutions of different volumes and different concentrations. Results indicate that the volume and concentration of the storage solution and the conditioning temperature will influence the rate of leaching, which is primarily related to the difference in ionic concentration between the pore and storage solutions. Furthermore, it was demonstrated through numerical simulations that microstructural properties (formation factor) can be used to characterize the rate of leaching.

The second phase of this study utilized cores of siltstone to demonstrate that the leaching of the ionic species can influence electrical measurements and even how different measurements (surface and uniaxial resistivity in this study) are related. An increase in specimen resistivity was observed, which was attributed purely to the leaching of the ionic species. Furthermore, the ratio of surface to uniaxial resistivity, which has been employed to indicate material homogeneity by Spragg [11], was shown to decrease as the leaching happens, but after sufficient leaching the value once again approach the initial value near 1. This suggests that after a sufficient amount of leaching, the material is again homogeneous, but the pore solution is much less concentrated than it was initially. The use of this resistivity ratio may be an effective way of evaluating the presence of on-going leaching.

The effects of leaching on electrical measurements on cementitious materials were discussed through the use of a diffusion model. Without consideration of binding or dissolution, and considering the storage solution as similar to tap water, the pore solution resistivity was estimated to increase up to three times its original value, and the ratio of the surface resistivity to the bulk resistivity decreased by as much as 10 % at room temperature.

In conclusion, this study has demonstrated that the leaching of ionic species occurs when samples are immersed in a fluid during curing and can drastically influence electrical measurements. The influence of these effects needs more evaluation for the impact on acceptance measurements for concrete projects, but their effects should be considered in current evaluations and in future standardization efforts. Methods such as moist-room curing could reduce the leaching (research has suggested that leaching can occur due to the water that condenses on the surface of a specimen in a moist room) or sealed curing would eliminate leaching [11,29]. However, additional corrections could be needed for the degree of saturation [22]. Additionally, these concretes (e.g., sealed cured or cured in a moist room) have exhibited good agreement between surface and uniaxial resistivity measurements at ages of 1 d, 7 d, 28 d, and 90 d for a variety of OPC and high-volume fly ash concretes [11,52].

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accuracy of the data presented herein, and do not necessarily reflect the official views or policies of the Federal Highway Administration and the Indiana Department of Transportation, nor do the contents constitute a standard, specification, or regulation. The authors would like to acknowledge helpful discussions from Professor Sidney Diamond and Professor Farshad Rajabipour.

## 7 References

- [1] W.J. McCarter, M.C. Forde, H.W. Whittington, Resistivity Characteristics of Concrete., ICE Proc. 71 (1981) 107–117. doi:10.1680/iicep.1982.1993.
- [2] E.J. Garboczi, Permeability, diffusivity, and microstructural parameters: A critical review, Cem. Concr. Res. 20 (1990) 591–601. doi:10.1016/0008-8846(90)90101-3.
- [3] C. Andrade, Calculation of chloride diffusion coefficients in concrete from ionic migration measurements, Cem. Concr. Res. 23 (1993) 724–742. doi:10.1016/0008-8846(93)90023-3.
- [4] W. Elkey, E. Sellevold, Portland Cement Concrete Pavement Permeability Performance, Directorate of Public Roads, Norwegian Road Research Laboratory, Oslo, 1995.
- [5] R.B. Polder, Test methods for on site measurement of resistivity of concrete - a RILEM TC-154 technical recommendation, Constr. Build. Mater. 15 (2001) 125–131. doi:10.1016/S0950-0618(00)00061-1.
- [6] R. Kessler, R. Powers, M. Paredes, Resistivity Measurements of Water Saturated Concrete as an Indicator of Permeability, in: NACE International, 2005.
- [7] A.A. Ramezani-pour, A. Pilvar, M. Mahdikhani, F. Moodi, Practical evaluation of relationship between concrete resistivity, water penetration, rapid chloride penetration and compressive strength, Constr. Build. Mater. 25 (2011) 2472–2479. doi:10.1016/j.conbuildmat.2010.11.069.
- [8] L. Tang, L. Nilsson, B.P. Basheer, Resistance of concrete to chloride ingress: testing and modelling, Spon Press, London ; New York, 2012.

- 735 [9] T.T. Rupnow, P. Icenogle, Evaluation of Surface Resistivity Measurements as an Alternative  
736 to the Rapid Chloride Permeability Test for Quality Assurance and Acceptance, Louisiana  
737 Department of Transportation, Baton Rouge, LA, LA, 2011.
- 738 [10] K.A. Snyder, The relationship between the formation factor and the diffusion coefficient  
739 of porous materials saturated with concentrated electrolytes: theoretical and  
740 experimental considerations, *Concr. Sci. Eng.* 3 (2001) 216–224.
- 741 [11] R.P. Spragg, The Rapid Assessment of Transport Properties of Cementitious Materials  
742 Using Electrical Methods, MSCE, Purdue University, 2013.
- 743 [12] N.S. Berke, M.C. Hicks, Estimating the life cycle of reinforced concrete decks and marine  
744 piles using laboratory diffusion and corrosion data, in: V. Chaker (Ed.), *Corros. Forms*  
745 *Control Infrastructure*, ASTM STP 1137, ASTM International, Philadelphia, Pennsylvania,  
746 1992: pp. 207–231.
- 747 [13] X. Feng, E. Garboczi, J. Bullard, D.P. Bentz, K. Snyder, P. Stutzman, T. Mason, Expanding a  
748 tool for predicting chloride diffusivity in concrete so it can be used by manufacturers to  
749 evaluate the durability of concrete made with blended cements. Part I: Characterizing  
750 blended cement materials., Gaithersburg, MD, 2004.
- 751 [14] E. Garboczi, D.P. Bentz, K. Snyder, N. Martys, P. Stutzman, C. Ferraris, J. Bullard, An  
752 electronic monograph: MODELING AND MEASURING THE STRUCTURE AND PROPERTIES  
753 OF CEMENT-BASED MATERIALS, Gaithersburg, MD, 2011.
- 754 [15] L. Yuan-Hui, S. Gregory, Diffusion of ions in sea water and in deep-sea sediments, *Geochim.*  
755 *Cosmochim. Acta.* 38 (1974) 703–714. doi:10.1016/0016-7037(74)90145-8.
- 756 [16] F. Rajabipour, Insitu electrical sensing and material health monitoring in concrete  
757 structures, PhD, Purdue University, 2006.
- 758 [17] H.F.W. Taylor, A method for predicting alkali ion concentrations in cement pore solutions,  
759 *Adv. Cem. Res.* 1 (1987) 5–17. doi:10.1680/adcr.1987.1.1.5.
- 760 [18] K. Snyder, X. Feng, B. Keen, T. Mason, Estimating the electrical conductivity of cement  
761 paste pore solutions from  $\text{OH}^-$ ,  $\text{K}^+$  and  $\text{Na}^+$  concentrations, *Cem. Concr. Res.* 33 (2003)  
762 793–798.
- 763 [19] D.P. Bentz, A virtual rapid chloride permeability test, *Cem. Concr. Compos.* 29 (2007) 723–  
764 731. doi:10.1016/j.cemconcomp.2007.06.006.
- 765 [20] M.R. Nokken, R.D. Hooton, Using pore parameters to estimate permeability or  
766 conductivity of concrete, *Mater. Struct.* 41 (2007) 1–16. doi:10.1617/s11527-006-9212-y.

- 767 [21] N. Olsson, V. Baroghel-Bouny, L.O. Nilsson, M. Thiery, Non-saturated ion diffusion in  
768 concrete - A new approach to evaluate conductivity measurements, *Cem. Concr. Compos.*  
769 40 (2013) 40–47. doi:10.1016/j.cemconcomp.2013.04.001.
- 770 [22] R. Spragg, Y. Bu, K.A. Snyder, D.P. Bentz, J. Weiss, Electrical Testing of Cement-Based  
771 Materials: Role of Testing Techniques, Sample Conditioning, and Accelerated Curing,  
772 Purdue University, West Lafayette, Indiana, 2013. doi:10.5703/1288284315230.
- 773 [23] I. De La Varga, Increased Fly Ash Volume and Internal Curing in Concrete Structures and  
774 Pavements, PhD, Purdue University, 2013.
- 775 [24] R. Spragg, C. Villani, K. Snyder, D.P. Bentz, J.W. Bullard, J. Weiss, Factors That Influence  
776 Electrical Resistivity Measurements in Cementitious Systems, *Transp. Res. Rec. J. Transp.*  
777 *Res. Board.* 2342 (2013) 90–98. doi:10.3141/2342-11.
- 778 [25] J. Weiss, K. Snyder, J. Bullard, D.P. Bentz, Using a Saturation Function to Interpret the  
779 Electrical Properties of Partially Saturated Concrete, *J. Mater. Civ. Eng.* 25 (2013) 1097–  
780 1106. doi:10.1061/(ASCE)MT.1943-5533.0000549.
- 781 [26] Y. Bu, J. Weiss, The influence of alkali content on the electrical resistivity and transport  
782 properties of cementitious materials, *Cem. Concr. Compos.* 51 (2014) 49–58.  
783 doi:10.1016/j.cemconcomp.2014.02.008.
- 784 [27] AASHTO TP95-11, Standard Method of Test for Surface Resistivity Indication of Concrete's  
785 Ability to Resist Chloride Ion Penetration, American Association of State Highway and  
786 Transportation Officials, Washington, D.C., 2011.
- 787 [28] R. Blanks, H. Meissner, The Expansion Test as a Measure of Alkali-Aggregate Reaction, *J.*  
788 *Am. Concr. Inst.* 42 (1946) 517–540.
- 789 [29] C. Rogers, R. Hooton, Reduction in Mortar and Concrete Expansion with Reactive  
790 Aggregates Due to Alkali Leaching, *Cem. Concr. Aggregates.* 13 (1991) 42.  
791 doi:10.1520/CCA10548J.
- 792 [30] C. Famy, K.L. Scrivener, A. Atkinson, A.R. Brough, Influence of the storage conditions on  
793 the dimensional changes of heat-cured mortars, *Cem. Concr. Res.* 31 (2001) 795–803.  
794 doi:10.1016/S0008-8846(01)00480-X.
- 795 [31] M. Thomas, B. Fournier, K. Folliard, J. Ideker, M. Shehata, Test methods for evaluating  
796 preventive measures for controlling expansion due to alkali-silica reaction in concrete,  
797 *Cem. Concr. Res.* 36 (2006) 1842–1856. doi:10.1016/j.cemconres.2006.01.014.

- 798 [32] P. Rivard, M. a. Bérubé, J.P. Ollivier, G. Ballivy, Decrease of pore solution alkalinity in  
799 concrete tested for alkali-silica reaction, *Mater. Struct.* 40 (2007) 909–921.  
800 doi:10.1617/s11527-006-9191-z.
- 801 [33] Muberra, F.P. Glasser, Long-term leaching mechanisms of Portland cement-stabilized  
802 municipal solid waste fly ash in carbonated water, *Cem. Concr. Res.* 29 (1999) 179–186.  
803 doi:10.1016/S0008-8846(98)00194-X.
- 804 [34] S. Diamond, Relevance of laboratory studies on delayed ettringite formation to DEF in field  
805 concretes, *Cem. Concr. Res.* 30 (2000) 1987–1991. doi:10.1016/S0008-8846(00)00390-2.
- 806 [35] C. Villani, R. Spragg, M. Pour-Ghaz, J. Weiss, The influence of pore solutions properties on  
807 drying in cementitious materials, *J. Am. Ceram. Soc.* 97 (2014) 386–393.  
808 doi:10.1111/jace.12604.
- 809 [36] C. Di Bella, Chloride transport and shrinkage of plain and internally cured concrete, MS,  
810 Purdue University, 2012.
- 811 [37] Y. Bu, R. Spragg, J. Weiss, Comparison of the Pore Volume in Concrete as Determined Using  
812 ASTM C642 and Vacuum Saturation, *Adv. Civ. Eng. Mater.* 3 (2014).  
813 doi:10.1520/ACEM20130090.
- 814 [38] B.J. Christensen, T. Coverdale, R.A. Olson, S.J. Ford, E.J. Garboczi, H.M. Jennings, T.O.  
815 Mason, Impedance Spectroscopy of Hydrating Cement-Based Materials: Measurement,  
816 Interpretation, and Application, *J. Am. Ceram. Soc.* 77 (1994) 2789–2804.  
817 doi:10.1111/j.1151-2916.1994.tb04507.x.
- 818 [39] R.P. Spragg, J. Castro, T. Nantung, M. Paredes, W.J. Weiss, Variability Analysis of the Bulk  
819 Resistivity Measured Using Concrete Cylinders, *Adv. Civ. Eng. Mater.* 1 (2012) 104596.  
820 doi:10.1520/ACEM104596.
- 821 [40] W. Morris, E.I.I. Moreno, A.A. Sagüés, Practical evaluation of resistivity of concrete in test  
822 cylinders using a Wenner array probe, *Cem. Concr. Res.* 26 (1996) 1779–1787.  
823 doi:10.1016/S0008-8846(96)00175-5.
- 824 [41] J. Bear, *Dynamics of Fluids in Porous Media*, Dover, New York, 1975.  
825 doi:10.1097/00010694-197508000-00022.
- 826 [42] R.B. Bird, W.E. Stewart, E.N. Lig, E.N. Lightfoot, *Transport Phenomena*, J. Wiley, New York,  
827 2013.
- 828 [43] R. Mills, V.M.M. Lobo, *Self Diffusion in Electrolyte Solutions: A Critical Examination of Data*  
829 *Compiled from the Literature*, Elsevier ; Distributors for the U.S. and Canada, Elsevier  
830 Science Pub. Co, Amsterdam ; New York : New York, NY, U.S.A, 1989.

- 831 [44] H. Mooney, E. Orellana, H. Pickett, L. Tornheim, A Resistivity Computation Method for  
832 Layered Earth Models, *Geophysics*. 31 (1966) 192–203.
- 833 [45] S.G. Millard, K.R. Gowers, Resistivity Assessment of in-Situ Concrete: the Influence of  
834 Conductive and Resistive Surface Layers., *Proc. ICE - Struct. Build.* 94 (1992) 389–396.  
835 doi:10.1680/istbu.1992.21502.
- 836 [46] S. Millard, Reinforced Concrete Resistivity Measurement Techniques., *Proc. Inst. Civ. Eng.*  
837 Part 2. 91 (1991) 71–88.
- 838 [47] Y. Liu, Experiments and Modeling on Resistivity of Multi-Layer Concrete With and Without  
839 Embedded Rebar, Florida Atlantic University, 2008.
- 840 [48] R. Spragg, C. Villani, J. Weiss, A. Pourasee, S. Jones, D.P. Bentz, K. Snyder, Surface and  
841 Uniaxial Electrical Measurements on Layered Cementitious Composites Having Cylindrical  
842 and Prismatic Geometries, in: *Proc. 4th Int. Conf. Durab. Concr. Struct.*, Purdue University,  
843 West Lafayette, IN, 2014: pp. 317–326. doi:10.5703/1288284315417.
- 844 [49] B.P.S. Rathor, H.S. Rathor, A resistivity computation method for layered earth models with  
845 transition boundary, *Pure Appl. Geophys. PAGEOPH.* 85 (1971) 153–160.  
846 doi:10.1007/BF00875405.
- 847 [50] R.T. Coverdale, H.M. Jennings, E.J. Garboczi, An improved model for simulating impedance  
848 spectroscopy, *Comput. Mater. Sci.* 3 (1995) 465–474. doi:10.1016/0927-0256(95)00005-  
849 B.
- 850 [51] R. Spragg, C. Villani, J. Weiss, Electrical Properties of Cementitious Systems : Formation  
851 Factor Determination and the Influence of Conditioning Procedures, *Adv. Civ. Eng. Mater.*  
852 5 (2016). doi:10.1520/ACEM20150035.
- 853 [52] D.P. Bentz, S.Z. Jones, K.A. Snyder, Design and performance of ternary blend high-volume  
854 fly ash concretes of moderate slump, *Constr. Build. Mater.* 84 (2015) 409–415.  
855 doi:10.1016/j.conbuildmat.2015.03.082.

856